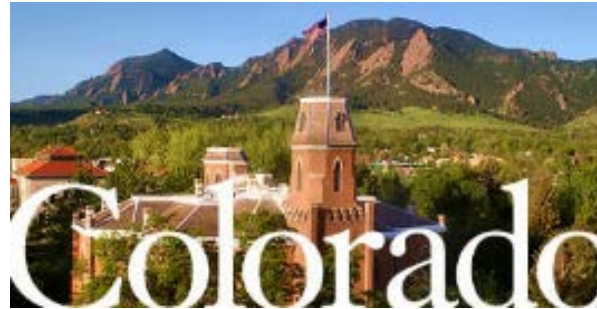


# MFIX-DEM Enhancement for Industry-Relevant Flows



Annual Project Review  
Meeting for Crosscutting, Rare  
Earth Elements, Gasification  
and Transformative Power  
Generation

Pittsburgh, PA  
April 2019

## Project leads

*Dr. Ray Cocco (PSRI, co-PI)*

*Dr. Ray Grout (NREL, co-PI)*

*Prof. Thomas Hauser (Univ. CO, co-PI)*

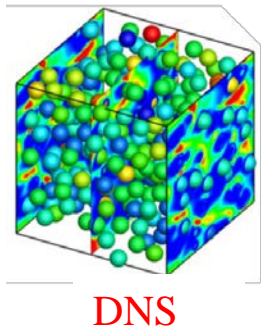
*Prof. Christine Hrenya (Univ. CO, PI)*

## Funding

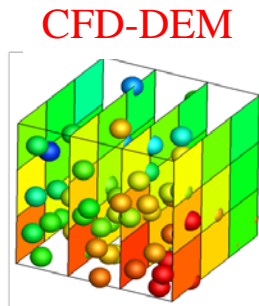


# Background: Numerical Methods for Studying Gas-solid Flows

Tenneti &  
Subramaniam (2016)

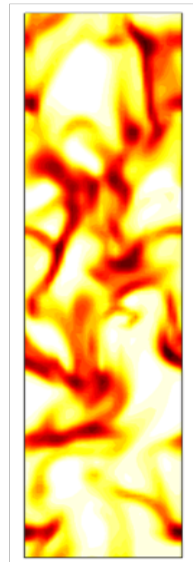


DNS



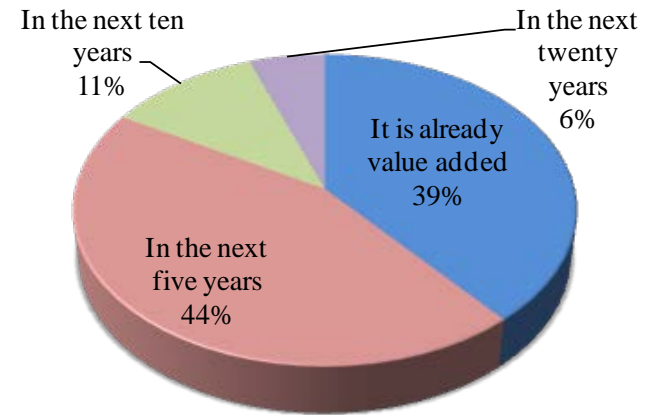
In-house

Two-Fluid Model  
(TFM)



In-house

Expected value added through DEM



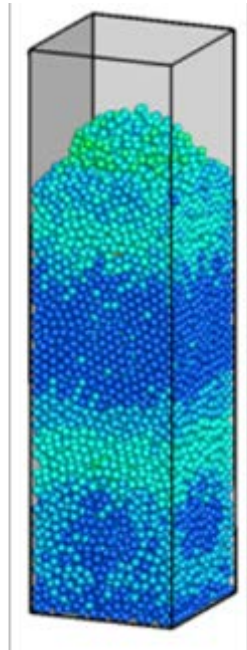
PSRI Industrial Survey  
(Cocco et al., *Chem. Eng. Prog.*, 2017)

← *More detail, fewer closures*

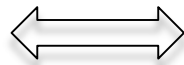
*Less CPU time* →

**DEM:**  
a balance between computational overhead and sources of uncertainty

# Motivation: Big picture



CFD-DEM  
 $N_p \sim 10^5 - 10^7$



Laboratory  
 $N_p \sim 10^9 - 10^{10}$



Industry  
 $N_p \sim 10^{14}$

**Goal: DEM application toward industrially relevant flows**

## Challenges

- Speed  $\Rightarrow$  Optimization & Algorithms (this talk)
- Results reliability  $\Rightarrow$  Validation & **Uncertainty Quantification (this talk)**

# Team

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## University of Colorado Chemical & Biological Engineering

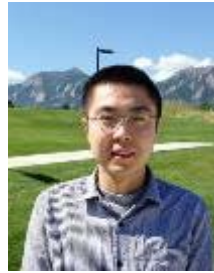
*DEM modeling of granular and gas-solid flows, MFIX*



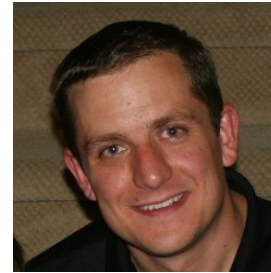
**Prof. Christine  
Hrenya**



**Dr. William Fullmer  
(now at NETL)**



**Dr. Peiyuan Liu**



**Dr. Steven Dahl**

## University of Colorado Research Computing

*High-performance  
computing, CFD*



**Prof. Thomas Hauser**



**Shadong Lao**

## NREL

### Computational Science

*High-performance computing, CFD*



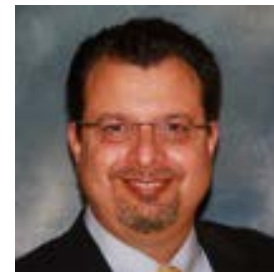
**Dr. Ray Grout**



**Dr. Hari Sitaraman**



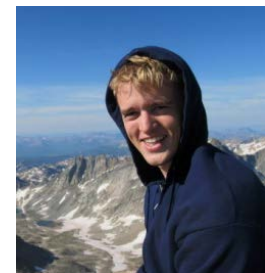
**Deepthi  
Vaidhynathan**



**Dr. Ray Cocco**



**Dr. Casey LaMarche**



**Aaron Holt**

## PSRI

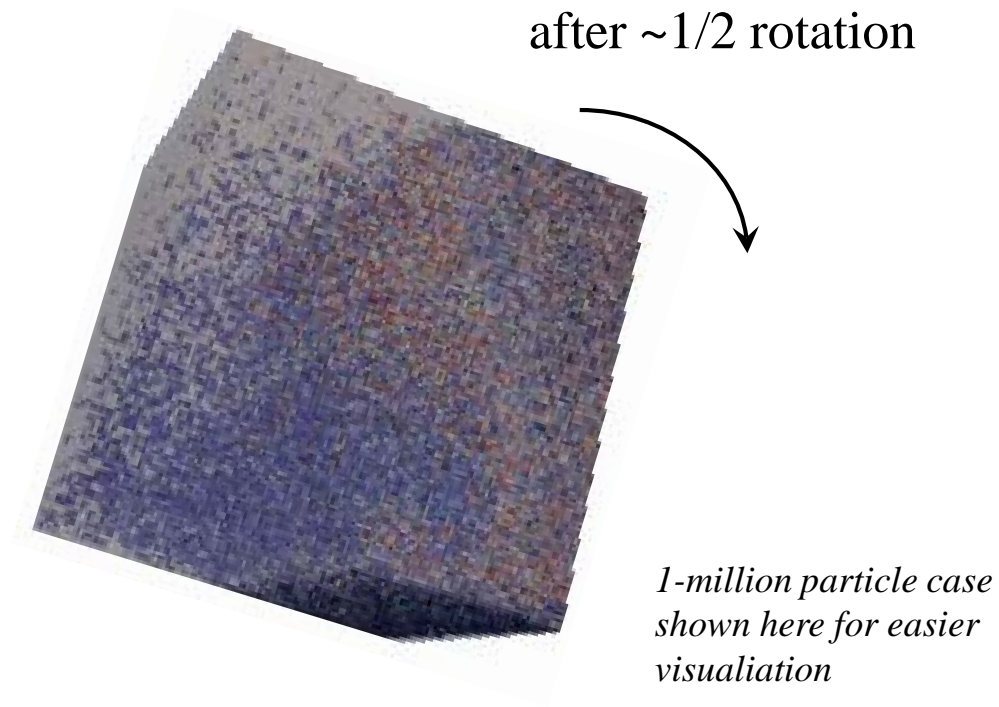
*Industrial Application and  
Experiments of Particle  
Flows*

# Recent Accomplishment: 1-billion particle case

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## Rotating square tumbler

- Gaussian PSD (250-750  $\mu\text{m}$ )
- Domain: 0.72m x 0.72m x 0.72 m
- Simulation time: 1 sec (1 full rotation)



# Background

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## Computer models are often deterministic

- One set of inputs → one set of outputs

## Most real-world problems include input uncertainty

- Measurement precision
- Natural variability (e.g., particle size distribution)

## State-of-the-art Uncertainty Quantification (*Full UQ*)

- Direct sampling over the entire phase-space of uncertain inputs
- Establishes range and likelihood of possible outcomes
- Often exceedingly expensive (*thousands of simulations; many more than validation*)

## Need to reduce computational expense to apply UQ to CFD-DEM

- *Reduced UQ*
  - Identify and propagate uncertainties for key input parameters only

# CFD-DEM Small-Scale Experiments: Prior Work

## Common system

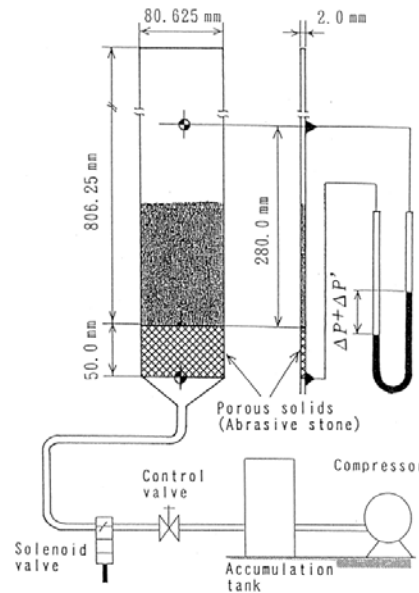
- *Small rectangular FB*
- *Group D particles*
- $N_p \sim 10^5$

## Metrics to compare

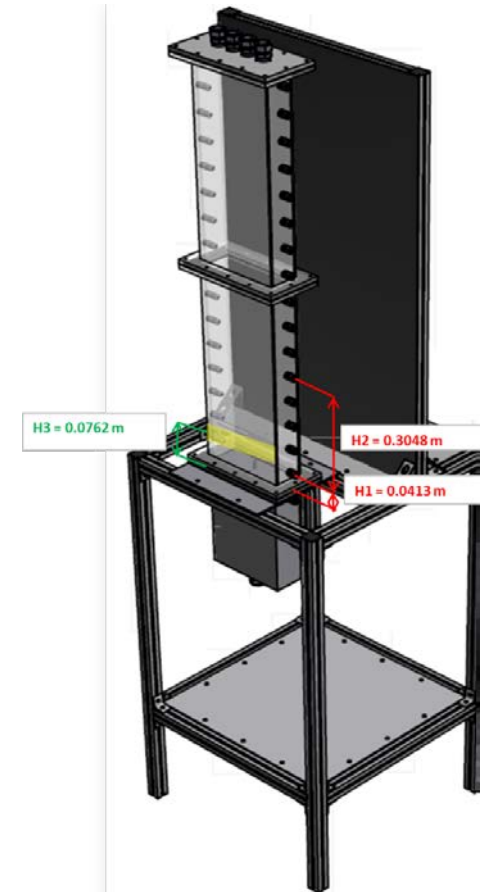
- *Flow patterns*
- *Pressure drop*
- *Velocity profiles*

## Objective

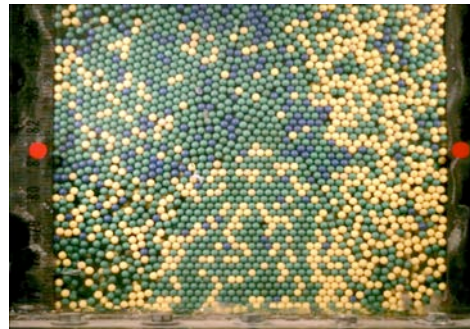
- *Code Validation*



(Yuu et al., *Powder Tech.*, 2000)



NETL Small-Scale Challenge (SSCP) Problem I  
(Gopalan et al., *Powder Tech.*, 2016)



Semi-circular bed with Horizontal Jets

(Fullmer, LaMarche, Issangya, Liu, Cocco & Hrenya, *AIChE J.*, 2018)

# Motivation and Objective: UQ effort

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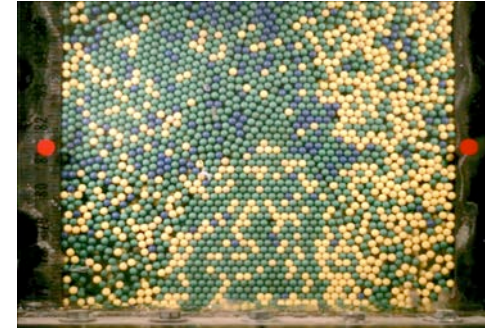
## Full UQ

### Epistemic Uncertainty – Unknown

- sample  $N^3+2$  epistemic uncertainties

### Aleatoric Uncertainty – Measured

- 100 samples/epistemic sample



- 60,000 particles
- 192 cpu hrs/simulation
- 5 epistemic uncertainties  
→ 12,700 Simulations

*To date, full UQ of CFD-DEM prohibitive*

## Current Objectives

1. Design experiment in which Full and Reduced UQ can be performed
2. Directly test Full UQ vs. Reduced UQ using **MFIX** DEM



# Experimental Design

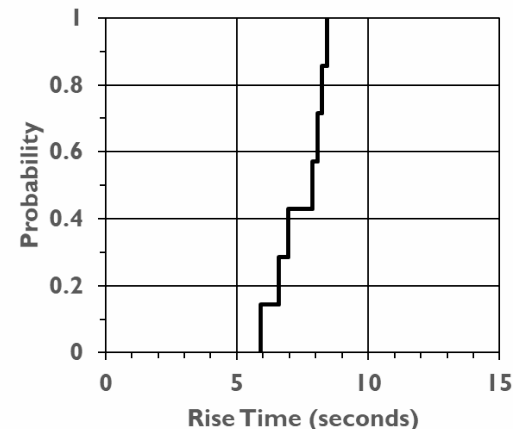
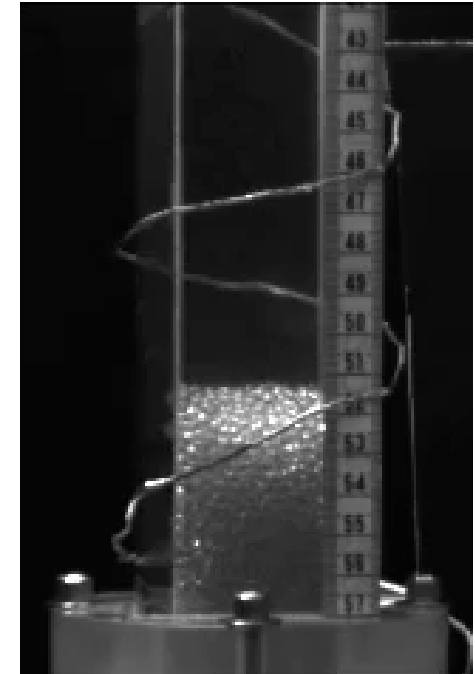
**Target:** Very-very small scale challenge problem (VVSSCP) with simulation times < 8 hours on a single CPU

## Important Considerations:

- Fast experiment: ~10 s or less
- Small # of particles:  $O(1,000)$  particles
- Careful characterization: *input uncertainty*
- Robustness
  - Particle-particle interaction important
  - Particle-fluid interaction important
  - Experimental results sensitive to some inputs

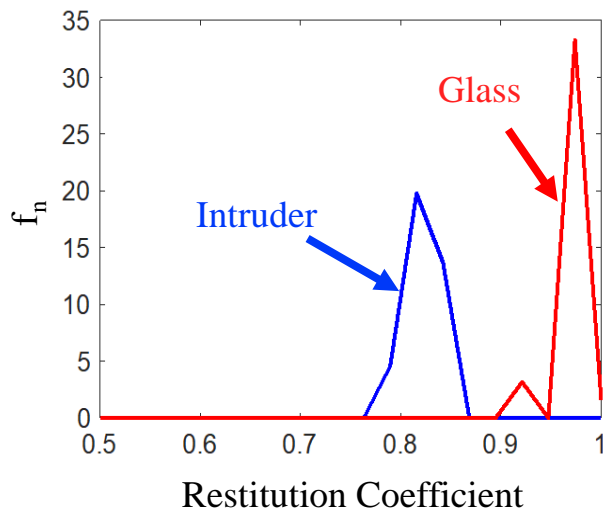
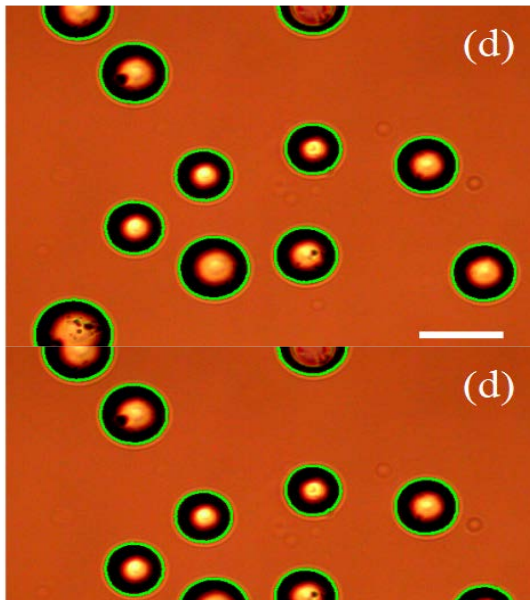
## System: Segregating Bed

- Glass particles in bed (~4300, ~3.1 mm dia.)
- HDPE particle (~9.4 mm dia.)
- Measurement: rise time
- Repeats to establish *output uncertainty*

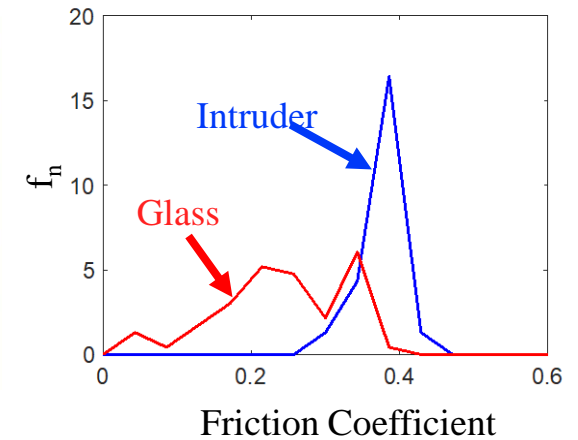
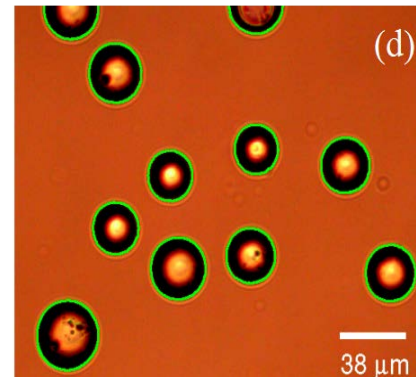


# Experiments: Aleatory Uncertainty (Particle Characterization)

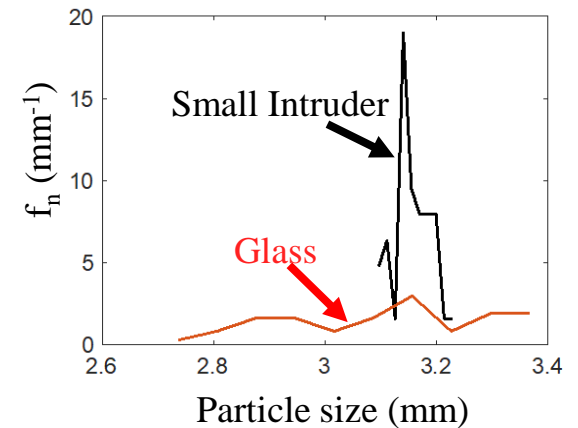
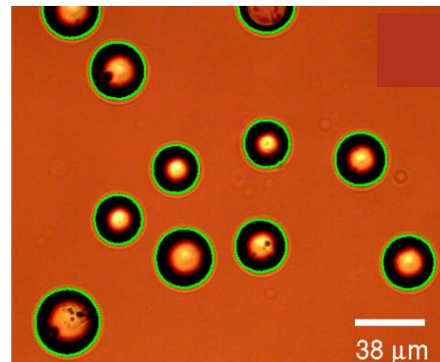
## Coefficient of Restitution



## Coefficient of Friction



## Size and shape



# Effort 1 – Segregating Bed

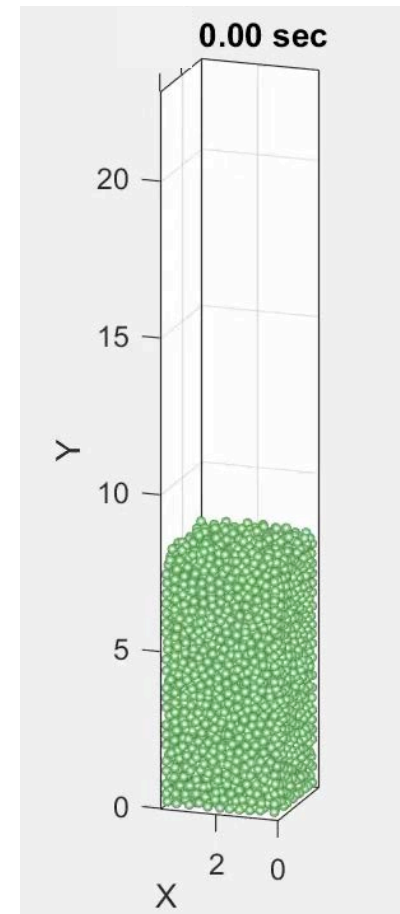
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## Objective

- Replicate experiments with CFD-DEM
- Apply *Full UQ* and *Reduced UQ* techniques



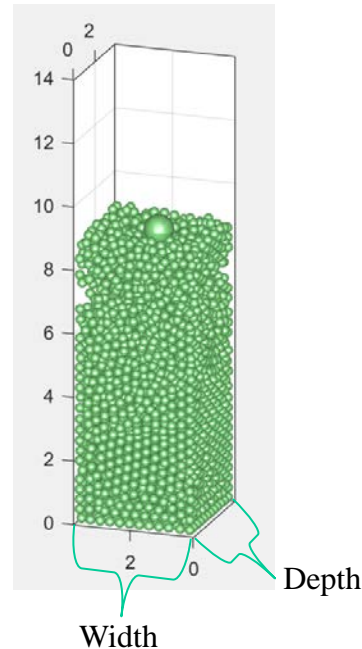
- Release 2016.1
- CFD-DEM
  - Soft-sphere
  - Free-slip wall (gas phase)
  - Rectangular grid
- Segregation time as key output



# Effort 1 – Uncertain Model Inputs

## Sources of uncertainty

Particle-phase Properties	
HDPE diameter	A
HDPE material density	E
Glass diameter	A
Glass material density	E
Glass-glass coefficient of restitution	A
Glass-wall coefficient of restitution	A
Glass-HDPE coefficient of restitution	A
Sphericity	A
Particle-particle coefficient of friction	A
Particle-wall coefficient of friction	A



Gas-phase Properties	
Gas rate variance	E
Outlet gas pressure	E
Inlet gas temperature	E

Dependent or Known Inputs	
Gas viscosity (via temperature)	
Nominal gas rate (via temp, pressure, nominal gauge readings)	
Total mass of glass particles (known)	
Bed depth & width (known)	

Aleatory = Natural variation, characterized by the measured CDF curve

Epistemic = Measurement precision, characterized as uniform probability between measured min & max

# Effort 1 – Full UQ

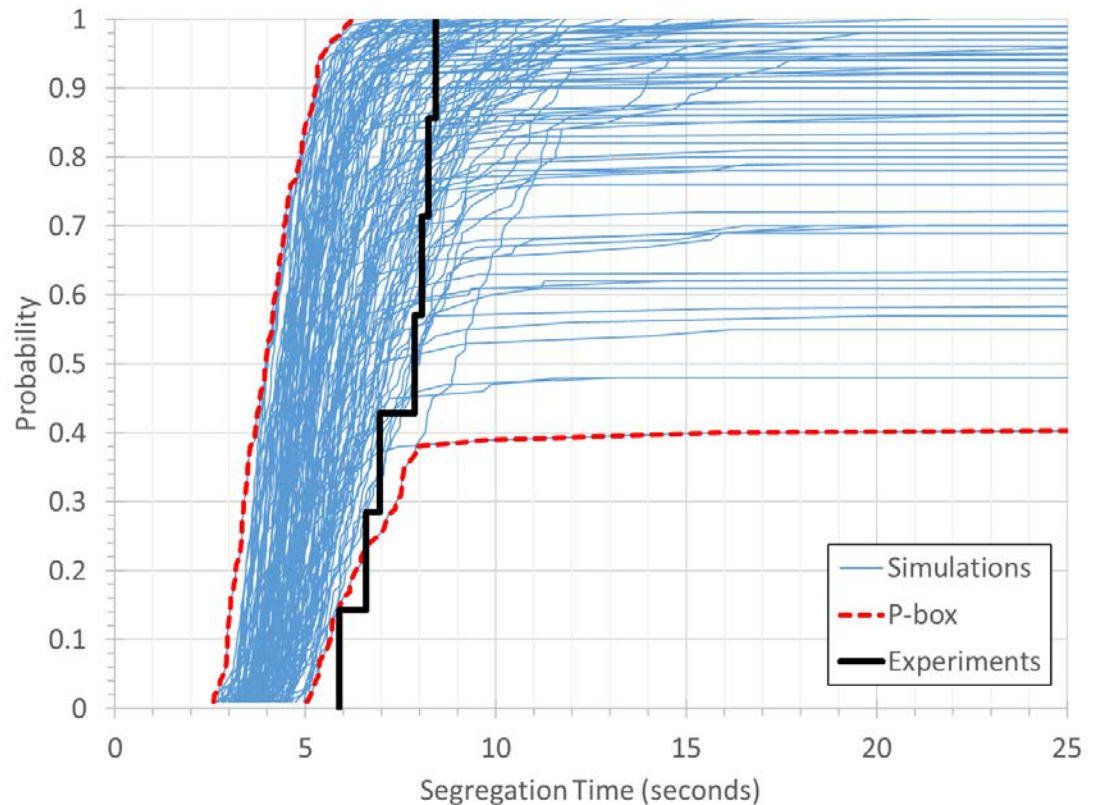
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## *Full UQ* input uncertainty propagation

- All input variables
- 127 epistemic points sampled
- 100 aleatory samples / epistemic point
- **12,700 simulations total**

## Results vs experiments

- Bias is for faster segregation in simulations

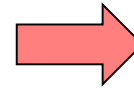


# Effort 1 – *Reduced UQ*

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## Sensitivity analysis

- Run base case
- Test high and low bounds for each input; hold others fixed
- Identify parameters that change output by >5%
- Eliminate others from forward propagation



## Investment

- 270 runs, 27 runs with 10 repeats of each to account for variation in initial conditions

## Uncertainty propagation

- Only influential variables
- 29 epistemic points sampled
- 100 aleatory samples / epistemic point
- **2,900 simulations total**

### Particle-phase Properties

HDPE diameter	A
HDPE material density	E
Glass diameter	A
Glass material density	E
Glass-glass coefficient of restitution	A
Glass-wall coefficient of restitution	A
Glass-HDPE coefficient of restitution	A
Sphericity	A
Particle-particle coefficient of friction	A
Particle-wall coefficient of friction	A

### Gas-phase Properties

Gas rate variance	E
Outlet gas pressure	E
Inlet gas temperature	E

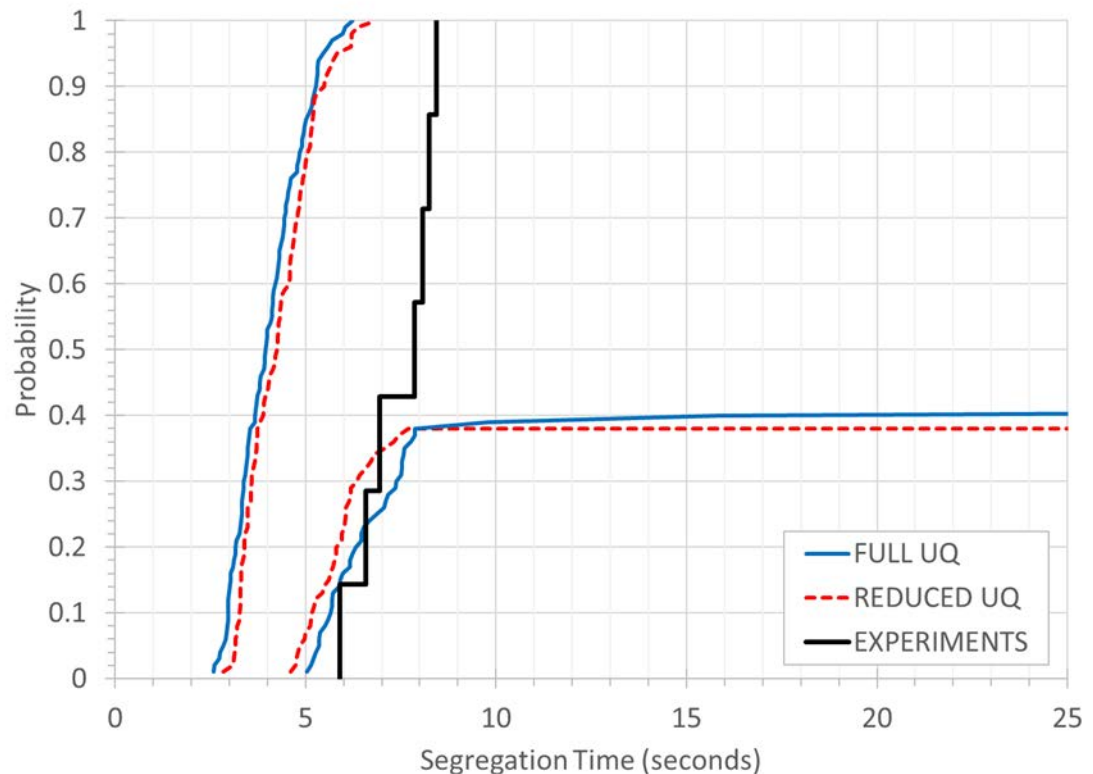
Aleatory = Natural variation

Epistemic = Measurement precision

# Effort 1 – Full UQ vs Reduced UQ

Direct comparison of forward propagation techniques

- Full UQ
  - 5 Epistemic variables
  - 8 Aleatory variables
  - 12,700 runs
- Reduced UQ
  - 3 Epistemic variables
  - 3 Aleatory variables
  - 3,170 runs
- Good agreement
  - 75% reduction in computational expense



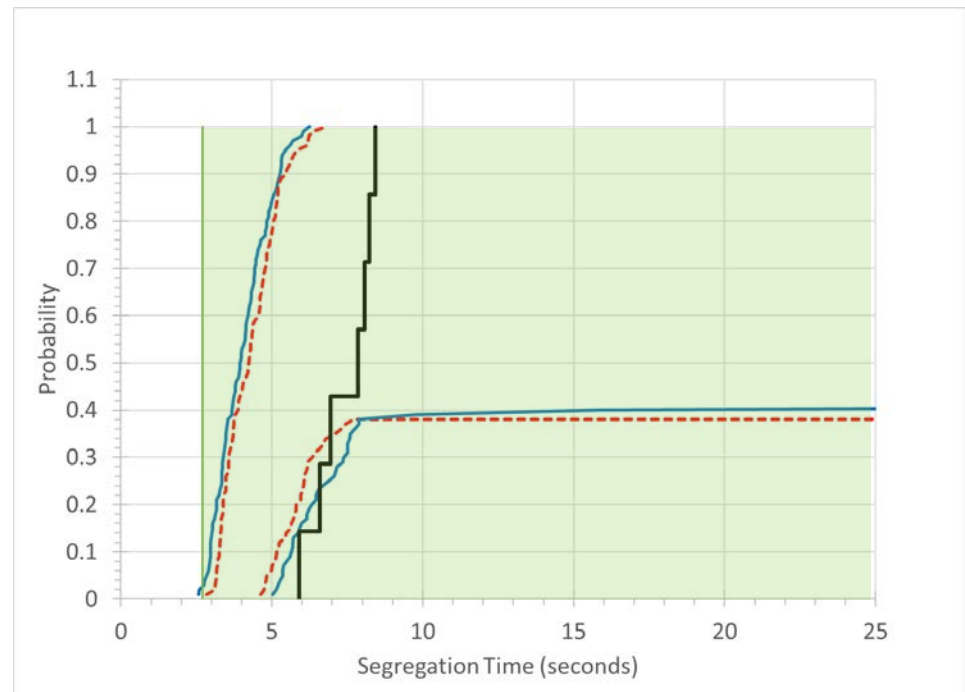
## Effort 1 – Conservative UQ

What happens if we just attempt to capture the extremes?

– *Conservative UQ*

- Use directional influence observed in sensitivity analysis (270 runs).
- Select combinations that should yield fastest and slowest segregation.
- 20 runs (2 points, with 10 repeats of each to account for initial conditions)

Method	Result	Runs
Conservative UQ	2.7 sec +	290
Reduced UQ	2.83 sec +	3170
Full UQ	2.58 sec +	12700





# Effort 2 – Mixing in Tumbler

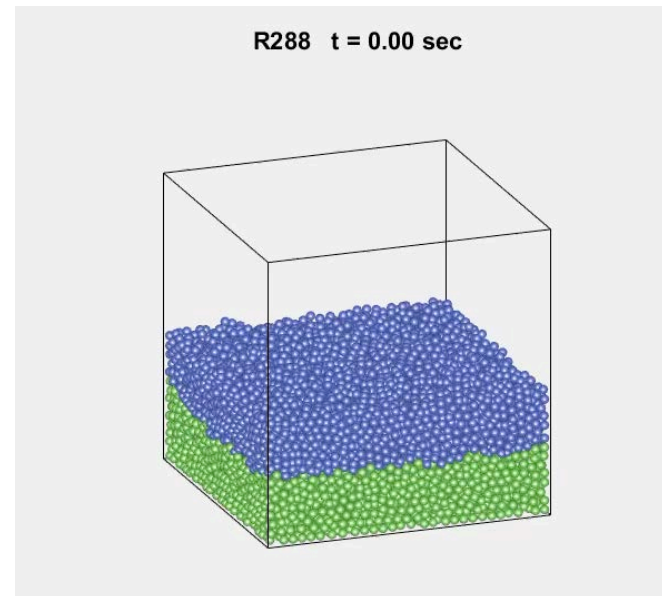
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## Objective

- Extend analysis to a second system with different physics



- Release 2016.1
- **DEM-only**
  - Soft-sphere
  - Rotating tumbler
  - Identical particles
  - Only color is different

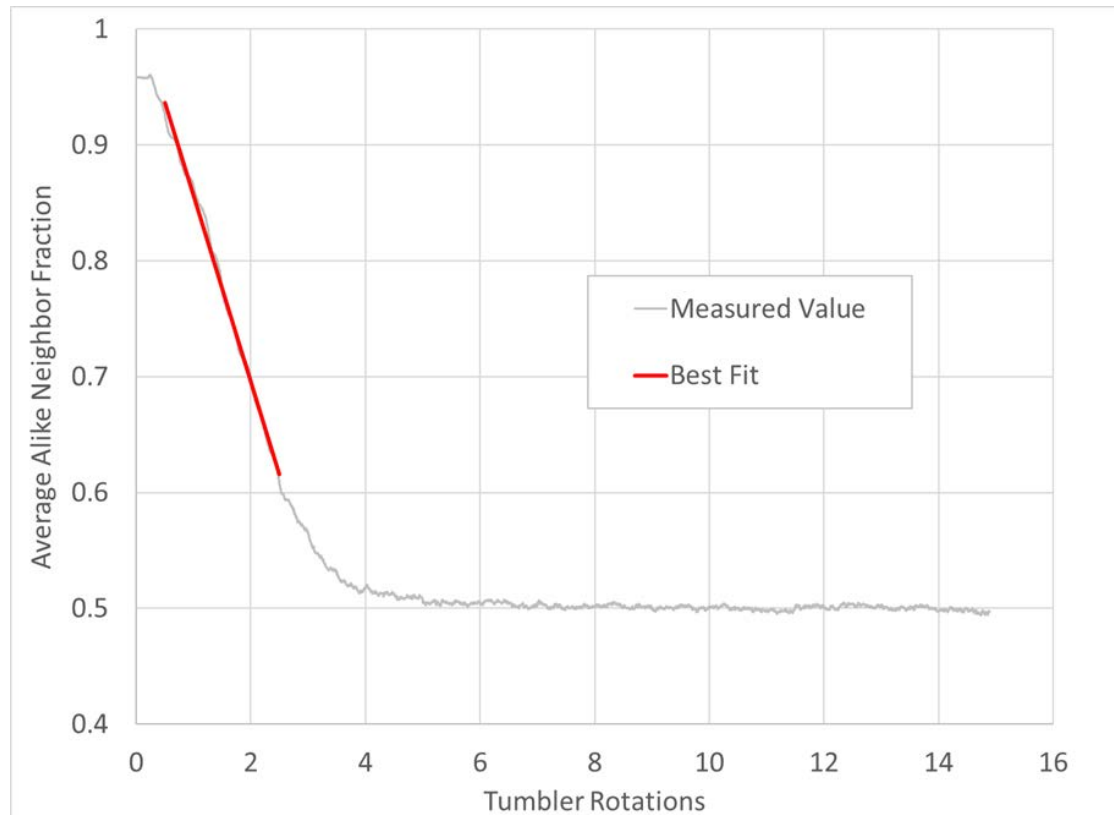


## Effort 2 – Mixing in Tumbler

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### Key output → initial rate of mixing

- Calculate “Alike Neighbor Fraction” (ANF) for each particle
- Calculate average ANF (including all particles with four or more neighbors)
- Focus on slope of best-fit line between 0.5- and 2.5- rotations.



# Effort 2 – Uncertain Model Inputs

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## Known Inputs

Tumbler dimensions  
 Total mass of glass particles  
 Acceleration due to gravity

## Full UQ

Uncertain Inputs	
Rotation rate	E
Glass diameter	A
Glass material density	E
Glass-glass coefficient of restitution	A
Glass-wall coefficient of restitution	A
Particle-particle coefficient of friction	A
Particle-wall coefficient of friction	A

## Reduced UQ

Uncertain Inputs	
Rotation rate	E
<del>Glass diameter</del>	<del>A</del>
Glass material density	E
Glass-glass coefficient of restitution	A
<del>Glass-wall coefficient of restitution</del>	<del>A</del>
Particle-particle coefficient of friction	A
Particle-wall coefficient of friction	A

Aleatory = Natural variation, characterized by the measured CDF curve

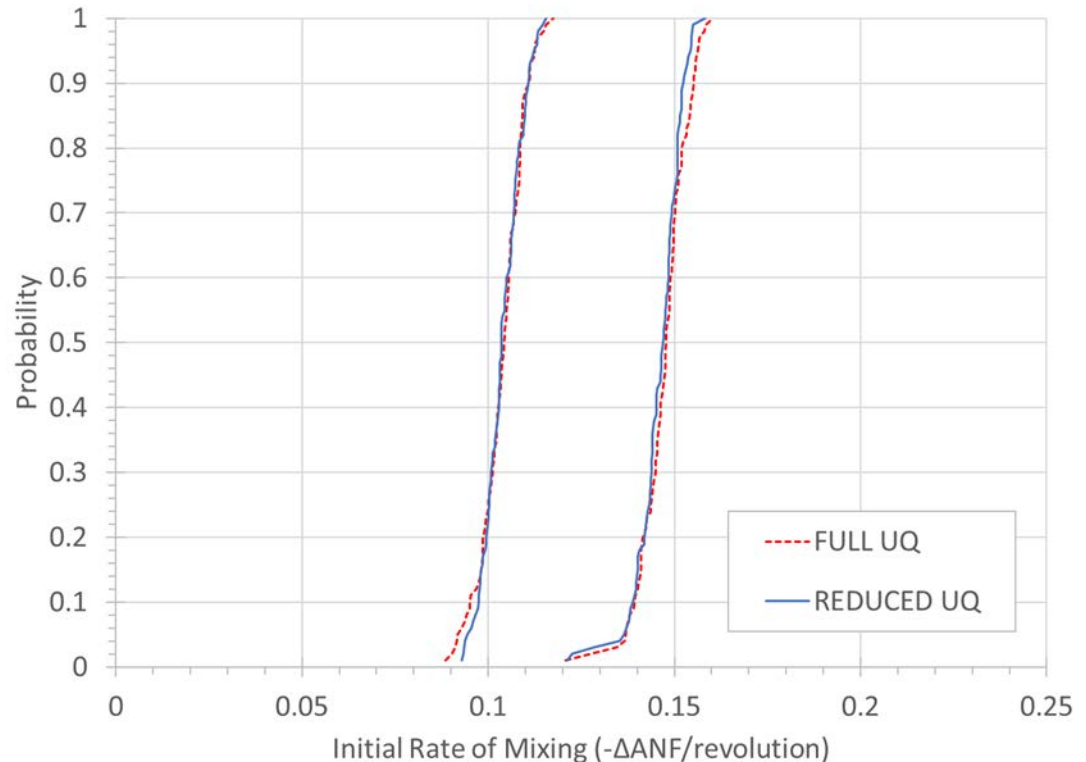
Epistemic = Measurement precision, characterized as uniform probability between measured min & max

## Effort 2 – Full UQ vs Reduced UQ

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Direct comparison of forward propagation techniques

- Full UQ
  - 2 Epistemic variables
  - 5 Aleatory variables
  - 1000 runs
- Reduced UQ
  - 1 Epistemic variable
  - 3 Aleatory variables
  - 345 runs
- Good agreement
  - 65% reduction in computational expense

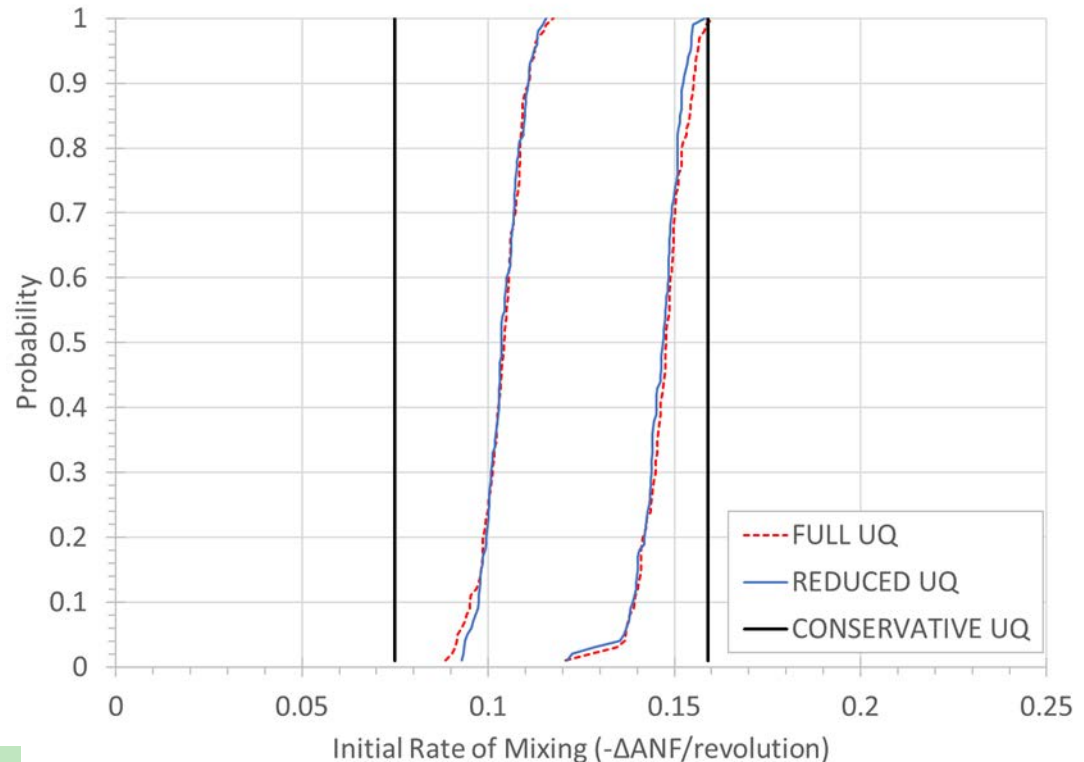


## Effort 2 – Conservative UQ

What happens if we just attempt to capture the extremes?

– *Conservative UQ*

- Use directional influence observed in sensitivity analysis (45 runs).
- Select combinations that should yield fastest and slowest mixing.
- 6 runs (2 points, with 3 repeats of each to account for initial conditions)



Method	Runs
Conservative UQ	51
Reduced UQ	345
Full UQ	1000

# Summary

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## Reduced UQ

- Performing a sensitivity analysis to eliminate insignificant input uncertainties can significantly reduce computational burden
  - NOTE: Systems in which all epistemic uncertainties are important would not benefit from a sensitivity-analysis since primary computational gains of *Reduced UQ* come from reducing epistemic uncertainties
- agreed well with *Full UQ* at 65%-75% computational savings

## Conservative UQ

- If only min/max output bounds are desired, using sensitivity analysis to guide inputs for min/max cases is promising
- agreed well with *Full UQ* for both efforts at a 95% computational savings