### Pulse Detonation Engine for Advanced Oxy-Combustion of Coal-Based Fuels

#### FE0025822

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### **Research Team**

#### Dr. David L. Blunck

- Experimental reacting flow studies and radiative heat transfer, 3 years as researcher at Air Force Researcher including collaboration with pressure gain combustion group

#### **Dr. Kyle Niemeyer**

- Numerical combustion research and detailed chemical kinetics

#### **Dr. Sourabh Apte**

- Large eddy simulations, turbulence modelling

# **Motivation**

- Improvements in thermal efficiency needed for power plants to address national energy challenges
- Pressure gain combustion can significantly improve efficiency
  - Pressure rise instead of pressure drop
  - Detonations often used
  - Unsteadiness of detonations challenging for turbomachinery
- Pulse detonation engine firing [2]
- Magnetohydrodynamics can provide step increase in thermal efficiency (e.g., 60% as part of topping cycle [1])
  - Operates better with high velocity and high temperature flows
  - Extract power from flow prior to entering turbomachinery



### **Motivation**



Illustration from prior detonation and MHD research [3]

- Prior (limited) research has considered detonations coupled with MHD, primarily for gaseous fuels
- Coal abundant resource in United States
- Little research investigating controlled detonations of coal (most research related to safety)
- Physical and thermal properties of coal detonations need to be measured to understand coupling with MHD

# **Technical Objectives**

#### **Overall Goal**

The overall goal of the effort is to develop and evaluate a pulse detonation combustion system for direct power extraction, or magnetohydrodynamic (MHD) system, and expand the existing pool of data for model validation of MHD systems.

#### **Specific Objectives:**

- 1) Design, build, and operate a pulse detonation engine intended for use with a MHD application. The device operates on gaseous or solid fuels with oxygen as the oxidizer.
- 2) Evaluate the operational envelope and performance of the pulse detonation device with particular focus on the inlet design and the ability to operate with both seeded and unseeded flows Experimental diagnostics will include the ability to measure the effect of the fuel type, seed material and detonation wave on the electromagnetic properties of the reacted gas flow.
- 3) Dévelop and validate a numerical design tool to calculate the performance of pulse detonation and coupled detonation-MHD systems.

### **Technical Background: Detonations**

- Supersonic flame front
- Detonation cells size characteristic of detonation properties
- High velocity ~ 2-3 km/s
- High temperatures ~3000K



- Illustration of detonation front [6]





Illustration of detonation cells [4]

### **Pulse Detonation Engine**



Illustration of pulse detonation cycle [7]

### **Coal Fired Pulse Detonation Engines**

Work performed by F.A. Bykovskii et al. [8]

- $H_2$ , air, coal
- 5–10 µm coal dust



Method for feeding detonation tube with coal [8]

## **Technical Background: Computations**

- Prior modeling studies on coal combustion at low speeds limited or no detonation
- Prior studies on coupled detonation–MHD systems: major simplifying assumptions
  - Neglected coupled electromagnetic fields & fluid transport
  - Omitting detailed models for combustion chemistry
  - Simple one-step ionization reactions for seed material

COLLEGE OF ENGINEERING

### **MHD Power Generation**

- Magnetohydrodynamic (MHD) power generation: electrically conductive fluid moving through a perpendicular magnetic field generates a current (*Faraday's Law of Induction*)
- Extracted power via MHD:  $P \propto \sigma imes V^2 imes B^2$
- Previously investigated as topping cycle, coupled with low-speed coal combustion [9]



Challenge: low speed requires significant pressure drop to increasevelocity9

### **MHD Power Generation**

- Potential benefits of detonation-fed MHD:
  - High velocities (Ma > 2) without pressure drop
  - High temperatures (T > 3000 K) increase electrical conductivity
- Prior research on detonation-MHD systems
  - Litchford et al. (NASA) & Cambier et al. (Air Force): MHD power extraction possible from propulsive PDE system [3,10,11]
  - Matsumoto et al. [12]: hydrogen-air PDE-powered MHD system
  - Major limitations:
    - Primarily propulsive systems; significant insight still needed into interactions between detonation and MHD field
    - Coal and natural gas significantly different than fuels studied (hydrogen)

# **CE/SE Methods for Pulse-Detonation**

#### **Basic approaches for reacting flows**

- Splitting Methods or Direct Methods
  - Both approaches based on Total Variation Diminishing (TVD) or Flux Corrected Transport (FCT) concepts
  - Upwinding with approximate Riemann solver for face fluxes
  - Flux or slope limiters to avoid numerical oscillations
  - Complicated algorithms in multi-dimension
- Conservation Element (CE)-Solution Element (SE) Method
  - Chang et al. (1999) for non-reacting flows (NASA Glenn) [13]
  - Integral form of conservation equations in space-time
  - No Riemann solvers
  - Fluxes balanced through careful selection of conservation cell locations
  - Gradients of flow variables treated as independent unknowns
  - A compact, conservative approach; at least second-order in time
  - Subcycling for chemical reactions (Wu et al. 2004) [14]

# **CE/SE Methods for Pulse-Detonation**

- Apply integral form of equation on conservation element (area ABCDEFG shown on right)
- Base solver from Wu et al. [14]
- H<sub>2</sub>–O<sub>2</sub> chemistry (9 species & 24 reactions; Franklach et al. [15])
- Validated for standard test cases
  - Incident shock-induced detonation
  - Stationary shock-induced detonation
  - 2D detonation
- Later used to study PDE flow dynamics and performance (Ma et al. [16–18])





### **CE/SE Method: 2D Detonation Example**



### **Overview of Research Approach**



### **Research Tasks**

- 1. Project Management and Planning
- 2. Build and Evaluate Pulse Detonation Combustor which Operates on Methane-Air and/or Methane-Oxygen
  - 2.1 Obtain design details and receive operational training
  - 2.2 Modify design for operation using oxygen and methane or gaseous fuels
  - 2.3 Build combustor and seeder
  - 2.4 Evaluative combustor performance
- **3. Build and Evaluate Pulse Detonation Combustor which Operates on Coal and Oxygen** 
  - 3.1 Modify design for operation using coal and air
  - 3.2 Build combustor for operation using coal and air
  - 3.3 Modify combustor for oxygen/coal detonations
  - 3.4 Evaluate combustor performance for coal detonations

### **Research Tasks**

4. Evaluate the Performance of a Coupled Pulse Detonation Engine and MHD Power Generator

- 4.1 Develop detonation code for oxy-coal
- 4.2 Develop MHD physics solver
- 4.3 Development and validation of a coupled oxy-coal detonation and MHD solver with parametric study

# Task 2: Design and Build a CH<sub>4</sub>/air/O<sub>2</sub> PDE



#### Task 2.1 – Visit AFRL (complete)

# Task 2.2 – Design and Operate PDE on gaseous fuels and oxygen

- Predetonator design from AFRL used to initiate detonations
- Single shot detonation tube to be built initially
- Extend tube to involve continuous pulse detonations (e.g., 1 Hz)
- Care taken using O<sub>2</sub>
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# Task 2: Design and Build a CH<sub>4</sub>/air/O<sub>2</sub> PDE



#### Task 2.3 – Design, build, and integrate seeder

- Will seed flow to increase conductivity
- Will establish design for coal seeder
- Seek to create uniform seed addition
- Will quantify changes in detonation characteristics when seeding present

# Task 2: Design and Build a CH<sub>4</sub>/air/O<sub>2</sub> PDE

#### **Task 2.4 – Evaluate detonation tube performance**

- Operate detonation tube with and without seeding, at different fuel-to-air ratios
- Quantify operation envelop and any challenges
- Measure detonation speed using ion probes (design obtained AFRL) and electrical conductivity/resistivity of the flow (equipment borrowed from NETL if needed)
- Estimate exhaust temperatures using infrared camera
- Data to validate calculations and provide boundary conditions, provide insights into detonations at different seeding and operating conditions, insights into coupling with MHD

# Task 3: Design and Build a Coal/air/O<sub>2</sub> PDE



# Tasks 3.1 and 3.2 – Design and build combustor to operate using coal and air

- Modify or adjust seeder design as needed
- Calibrate flow rates and seed characteristics
- Coal powder to be used, well characterize for models
- Dilution with carrier gas may be required to reduce cell sizes

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• Will seed with ionizing particles if needed

# Task 3: Design and Build a Coal/air/O<sub>2</sub> PDE



Tasks 3.3 – Design and build combustor to operate using coal and oxygen

- Reduced cell sizes possible
- High exhaust temperatures will result
- Measure detonation speeds with air or oxygen
- Care when considering combustion with oxygen

# Task 3: Design and Build a Coal/air/O<sub>2</sub> PDE

#### **Task 3.4 – Evaluate detonation performance**

- Operate detonation tube with coal powder, at different fuel-toair ratios
- Quantify operation envelope
- Measure detonation speed using ion probes (design obtained AFRL) and electrical conductivity/resistivity of the flow (equipment borrowed from NETL if needed)
- Estimate exhaust temperatures using infrared camera
- Data to validate calculations and provide boundary conditions, provide insights into detonations at different seeding and operating conditions, insights into coupling with MHD

#### **Task 4: Calculate Detonation and MHD Performance**

#### **Task 4.1 Develop detonation code**

- Convert the original CE/SE solver to Fortran 90 or C
- Incorporate simplified reduced reaction kinetics for oxyfuel combustion
- Implicit treatment and subcycling for reacting source terms
- Verification and validation against experiment

Jones-Lindstedt Mechanism with Dissociation Reactions (JL-R) Reaction Reaction rate

	Kacuon	Reaction rate
1	$CH_4 + \frac{1}{2}O_2 \longrightarrow CO + 2H_2$	$r_1 = 4.4 \cdot 10^{11} e^{-\frac{30000}{RT}} \left[ CH_4 \right]^{0.50} \left[ O_2 \right]^{1.25}$
2	$CH_4 + H_2O \longrightarrow CO + 3H_2$	$r_2 = 3 \cdot 10^8 e^{-\frac{30000}{RT}} [CH_4] [H_2O]$
3	$\rm CO + H_2O \longrightarrow CO_2 + H_2$	$r_3 = 2.75 \cdot 10^9 e^{-\frac{20000}{RT}} [CO] [H_2O]$
4	$H_2 + 0.5O_2 \xrightarrow{\longrightarrow} H_2O$	$r_4 = 6.80 \cdot 10^{15} T^{-1} e^{-\frac{40000}{RT}} \left[H_2\right]^{0.25} \left[O_2\right]^{1.50}$
5	$O_2  2O$	$r_5 = 1.5 \cdot 10^9 e^{-\frac{113000}{RT}} [O_2]$
6	$H_2 O  H + OH$	$r_6 = 2.3 \cdot 10^{22} T^{-3} e^{-\frac{120000}{RT}} [H_2 O]$
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Frassoldati et al. [19]

 $\nabla \cdot \mathbf{B} = 0$ 

#### **Task 4: Calculate Detonation and MHD Performance**

#### Task 4.2 Development of MHD solver based on CE/SE method:

• Two-dimensional equations (conservative form)

$$\frac{\partial \mathbf{U}}{\partial t} + \frac{\partial \mathbf{F}}{\partial x} + \frac{\partial \mathbf{G}}{\partial y} = 0 \qquad \mathbf{U} = (\rho, \rho u, \rho v, \rho w, e, B_x, B_y, B_z)^T \\ \downarrow \\ \nabla \cdot \mathbf{h}_m = 0, \quad m = 1, 2, \dots, 8 \text{ Transformed via Gauss' divergence theorem, then} \\ \mathbf{h}_m = (f_m, g_m, u_m) \qquad \text{solved via standard CE/SE approach.}$$

- One complication: need to ensure
  - Follow extended CE/SE scheme proposed by Zhang et al. [20]

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- Benchmark test cases:
  - Rotated one-dimensional MHD shock tube problem
  - MHD vortex problem

#### **Task 4: Calculate Detonation and MHD Performance**

Task 4.3 Couple CE/SE-based detonation and MHD solvers, perform parametric study of oxy-coal PDE-MHD power generation system

**Necessary tasks:** 

- Develop coupled combustion & ionization chemistry model based on H<sub>2</sub>-O<sub>2</sub> model of Schulz et al. [21]
- Add electron-impact ionization, electron-impact dissociation, associative ionization and charge-exchange reactions
- Addition of KO<sub>2</sub>, KOH, KO, K, and single-step K ionization reaction

#### Validation against experiment:

- Detonation wave characteristics
- Properties of reacting/reacted flow with/without seed

#### **Task 4: Calculate Detonation and MHD Performance**

Task 4.3 Couple CE/SE-based detonation and MHD solvers, perform parametric study of oxy-coal PDE-MHD power generation system

#### **Topics to be investigated:**

- How much power can be extracted for different conditions?
- Effects of varying seed particle concentration, and determine optimum, for example Schulz et al. [21] found larger amounts of potassium seed interfered with detonation via radical competition
- Effect of fuel composition on detonation and MHD
- Explore possibility of seed-free operation through high detonation temperatures

# Deliverables

- Fundamental understanding about velocity and conductivity of detonation waves with and without seeding (insight into potential for MHD coupling)
- Calculated MHD performance when coupled with detonation tube
- Understanding about achieving coal fueled pulse detonations
- Peer reviewed articles (4+ estimated)
- Program management plan
- As requested:
  - Detonation tube with operating instructions
  - Code developed for project (excluding code obtained from collaborator without permission)

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- 3 MS/PhD students
- 4 undergraduate students with research experience (estimated)
- Final and mid-term reports

### **Experimental Facilities and Capabilities**

#### **Propulsion Laboratory**

- Located near edge of campus
- Remote test operation in control room
- High speed DAQ being installed
- Student desks and space available



**Picture within Propulsion Laboratory** 

#### **Measurement capabilities**

- Infrared camera (sensitive in mid-infrared, > 1 kHz possible)
- ICCD and high speed cameras available for measurements

### **Computational Facilities and Capabilities**

- Existing computational model for gas-phase PDE to be obtained from collaborator
- Expertise in Finite Volume Methods (compressible and incompressible formulation) for reacting flows
- Access to CE/SE solver for compressible, reacting flows
- Experience in oxyfuel-combustion mechanisms
- Expertise in particle-laden, turbulent flows (Euler–Lagrange and Eulerian two-fluid approaches)
- In-house parallel computing cluster (built in collaboration with NETL), a high memory data processing server & access to OSU College of Engineering High-Performance Computing cluster

#### **Collaborations and Synergies** Computational

- Interactions with Dr. Wu have been initiated to exchange the computational solver upon which the numerical modeling tool will be built
- Visiting graduate student from University of Tsukuba, Japan, with background in MHD simulations

#### Experimental

- Initial training and system design obtained from Innovative Scientific Solutions Inc.(ISSI)
- ISSI and Air Force Research Laboratory (AFRL) will continue to be a reference
- Dr. Rigel Woodside is building a MHD system at NETL in Albany, Oregon, will share results and use guidance

### **Progress to Date**

- Received training and designs from AFRL
  - Received training related to PDE operation and safety •
  - Designs for small detonation systems (pre-detonator)
- Revised predetonation design and acquiring materials
- Scheduled to have functional predetonation system by the end of the year • (used to initiate detonations)
- Started designs for single shot detonation tube
- Specifying data acquisition system ۲
- Laboratory prepared for detonation system ۲
- Acquired a 1D solver based on Space-Time methods with reduced reaction chemistry
  - The solver is for single processor and Fortran 77. Needs an upgrade to Fortran90 or C.
- Currently recruiting graduate student for the computational part of the research

# **Potential Challenges**

#### Experimental

- Valving and timing to achieve continuous operation, will work with AFRL as needed
- Coal air has relatively large detonation cells, may require dilution with  $H_2$  to achieve
- Coal feeding and distribution within detonation tube

#### Computational

- Coupling of flow dynamics and magnetohydrodynamics (space and time scale variations) using CE/SE method should facilitate coupling
- Recruitment of graduate student in progress

### Timeline

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