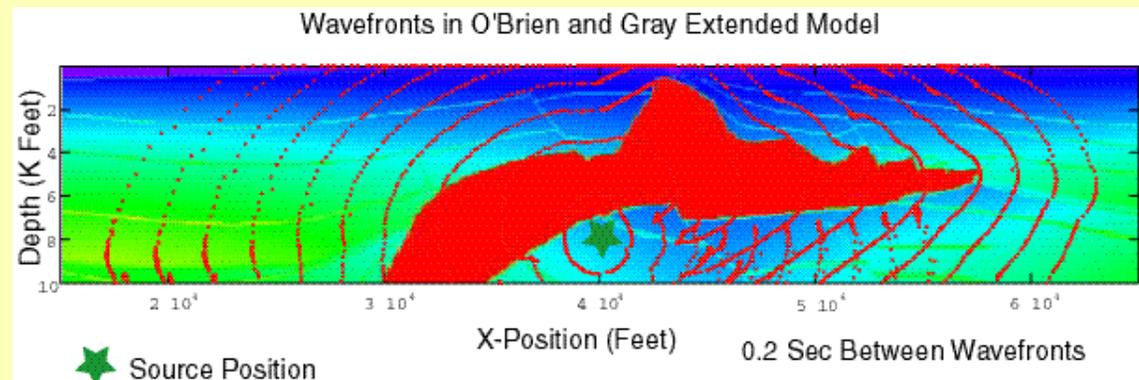


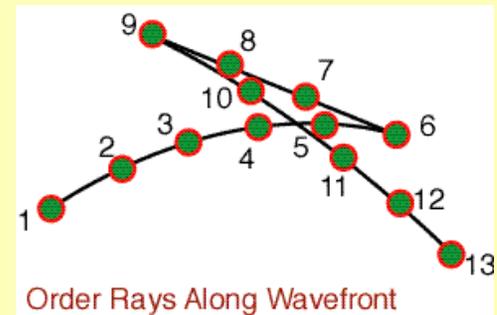
# Improved Prestack Kirchhoff Migration for Complex Structures

- Provide algorithm improvements to Kirchhoff migration
- Allow improvements to current Kirchhoff implementations
- Maintain computational advantage of Kirchhoff



# KIRCHHOFF MIGRATION

- 3D prestack migration important to image complex structures
- Kirchhoff most commonly used method today
  - » Kirchhoff computational requirement much less than alternatives
  - » Provides option for target oriented imaging
  - » Allows 3d prestack migration on computers available today
  - » In use at many companies



# KIRCHHOFF MIGRATION (Cont.)

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- Kirchhoff has problems in complex geologies
  - » Alternatives are more computationally intensive and benefits are not demonstrated
- Many groups are trying to improve Kirchhoff
  - » Technology for amplitude and phase is questionable
  - » Still problems with reliable traveltimes calculation
  - » Uncertainties in using multi-valued traveltimes

# Advantages of the Kirchhoff Migration Method

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- Rich history in industry so it is well understood and trusted
- Can do target-oriented imaging at a fraction of the cost of imaging an entire volume.
- Inexpensive generation of migrations for various offsets
- Computer memory requirements are less severe than some methods
- Ease of dealing with irregular source and trace spacing

# What is Unique about this Project?

We are investigating use of multiple arrivals  
in Kirchhoff Migration

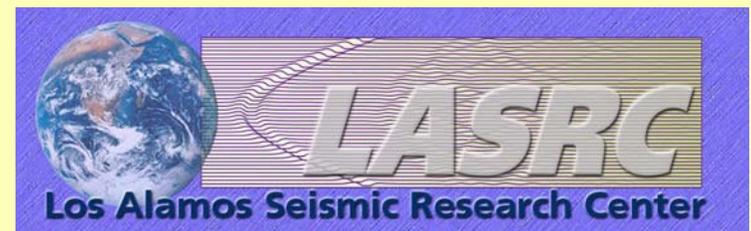
- » efficient generation of traveltimes tables
- » use of amplitudes and phases
- » currently doing target-oriented imaging for efficiency
- » Investigating data contributions and raytracing influences on image



# We have Developed a Numerical Testbench

Kirchhoff target oriented migration with  
wavefront construction

- ▼ Model multiple travel time arrivals
- ▼ Ray tracing using wavefront construction from image point
- ▼ Image seismic wavefield (no travel time table decimation, storage, or interpolation )



# Numerical Testbench

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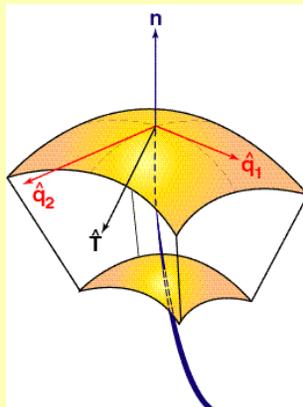
Study the impact on image due to

- amplitude
- phase
- coherence filtering
- minimum travel time
- maximum amplitude travel time
- different ray path legs

Use synthetic and real data sets

# Accomplishments

- New wavefront construction ray addition criteria
  - » Based on physics of ray theory
- Wavefront curvature estimate without solving dynamic ray equations



**Calculation of Curvature**

$$\text{Curvature} = \vec{T} \cdot d\vec{N}/ds = |\vec{X}_{n+1} - \vec{X}_n| \cdot (\vec{N}_{n+1} \cdot \vec{N}_n) / |\vec{X}_{n+1} - \vec{X}_n|^2$$

ds = Differential arc Length Along Wavefront  $\sim |\vec{X}_{n+1} - \vec{X}_n|$

$\vec{T}$  = Unit Tangent Vector =  $(\vec{X}_{n+1} - \vec{X}_n) / |\vec{X}_{n+1} - \vec{X}_n|$

$\vec{N}_n = \vec{P}_n / |\vec{P}_n| = v(\vec{X}_n) \vec{P}_n$

Wavefront construction: Slide 10 (right)

# Accomplishments

- Ray theory concepts
  - » wavefront entropy
  - » ray chaotic orbits (amplitude and phase unreliable)
  - » physical ray theory obtained via gauge transform of ray Hamiltonian

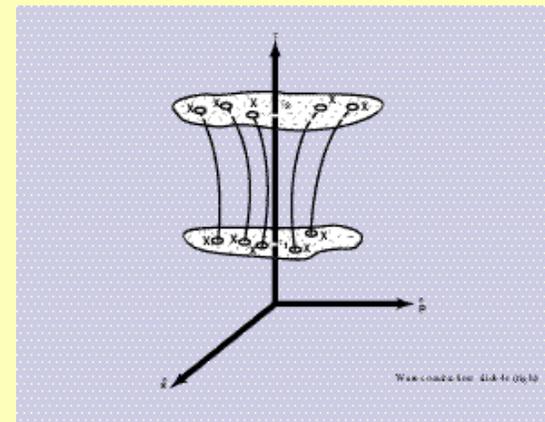
Ray theory from a differential geometry perspective

Hierarchical ray theory

Theory	Integral	Physics	Symmetry
Ray Bundle	point	phase space manifold, Hamiltonian	quadratic
Art	path	Fermat's Principle, Hamilton ray equations, $dH=0$	geodesic
Dynamic	surface	Liouville Theorem, transport equation, $d(dH)=0$	symplectic
Physical	volume	Fresnel zone, coherent scattering, $d(dH)=0$	gauge

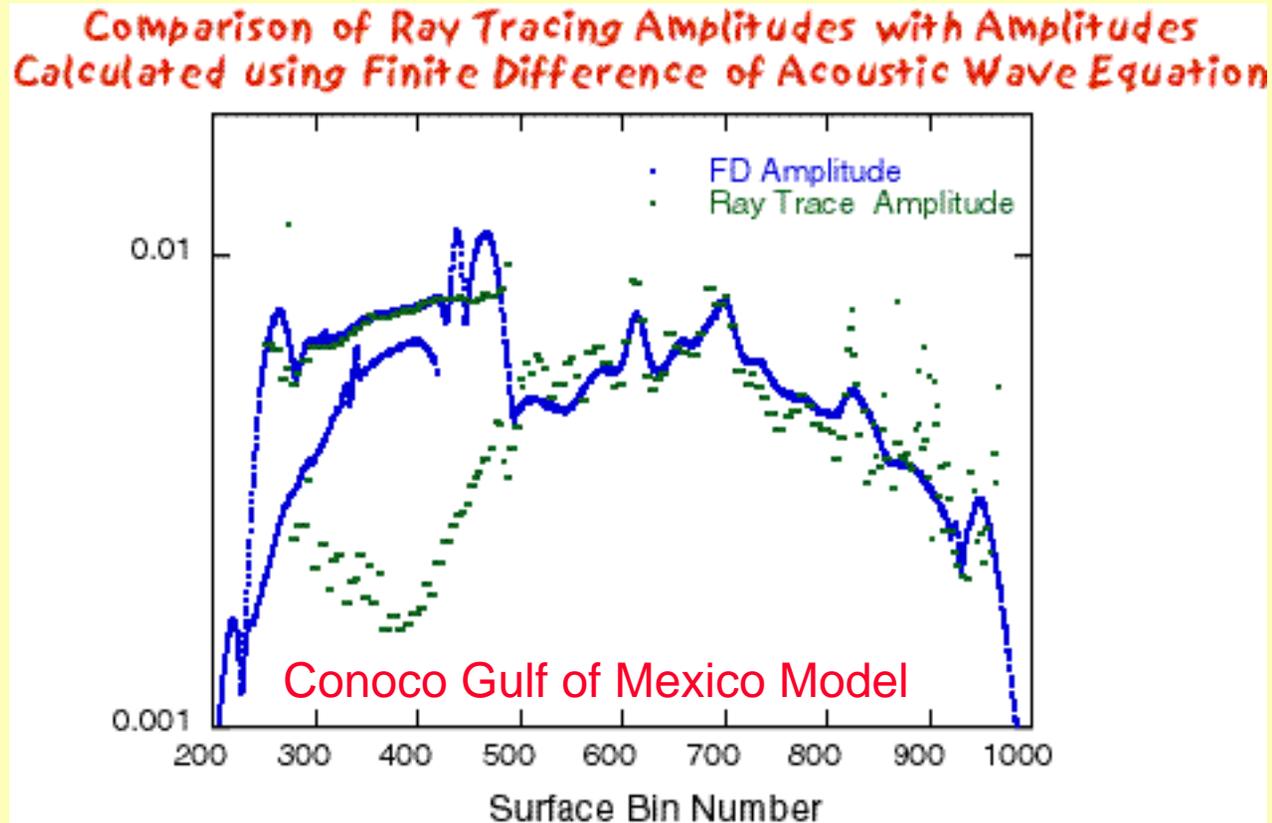
$H = 1/2 [p_x^2 + p_y^2 - u^2]$   
 $H = 1/2 [(p_x + (1/m)g(x,y))p_x + (1/m)g(x,y) - u^2]$  (Kleber and, 1997)

Wavefront construction  
 3d-4c-4d-5



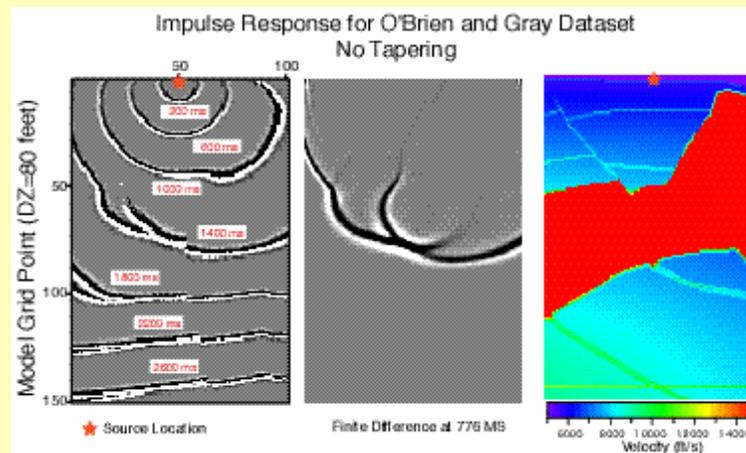
# Accomplishments

- Ray Amplitudes Validated

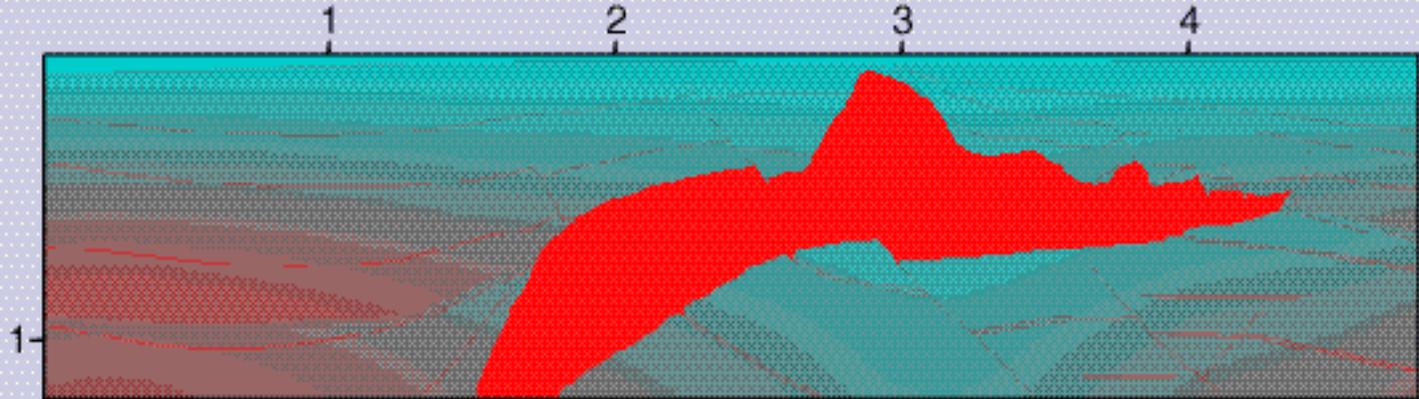


# Accomplishments

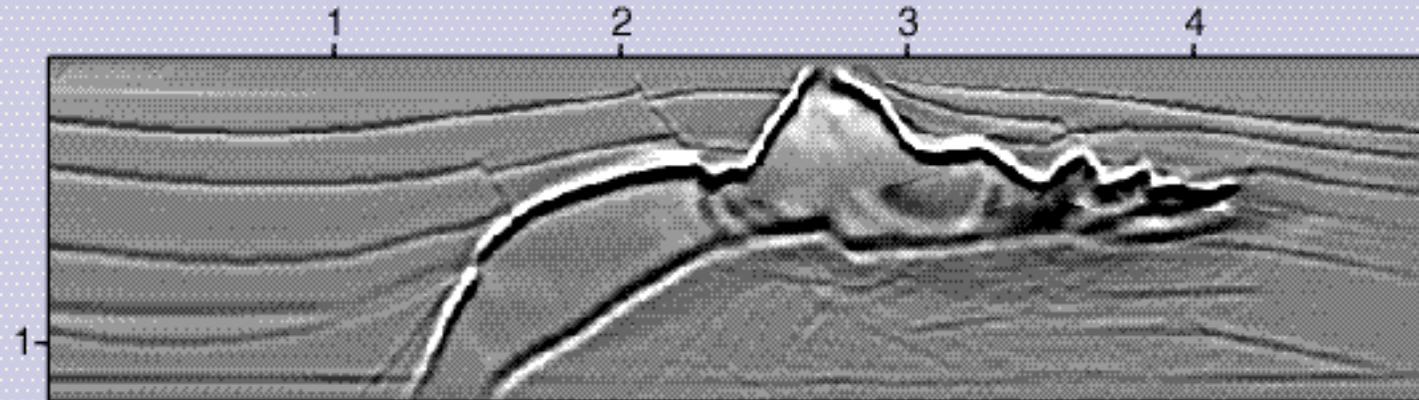
- Constant ray sigma step imaging
- Migration using wavefront construction
  - » Investigated impulse response
  - » Migrated real and synthetic data



O'Brien and Gray Model



Distances are \*10000 Feet



**Image Obtained using Wavefront Construction**

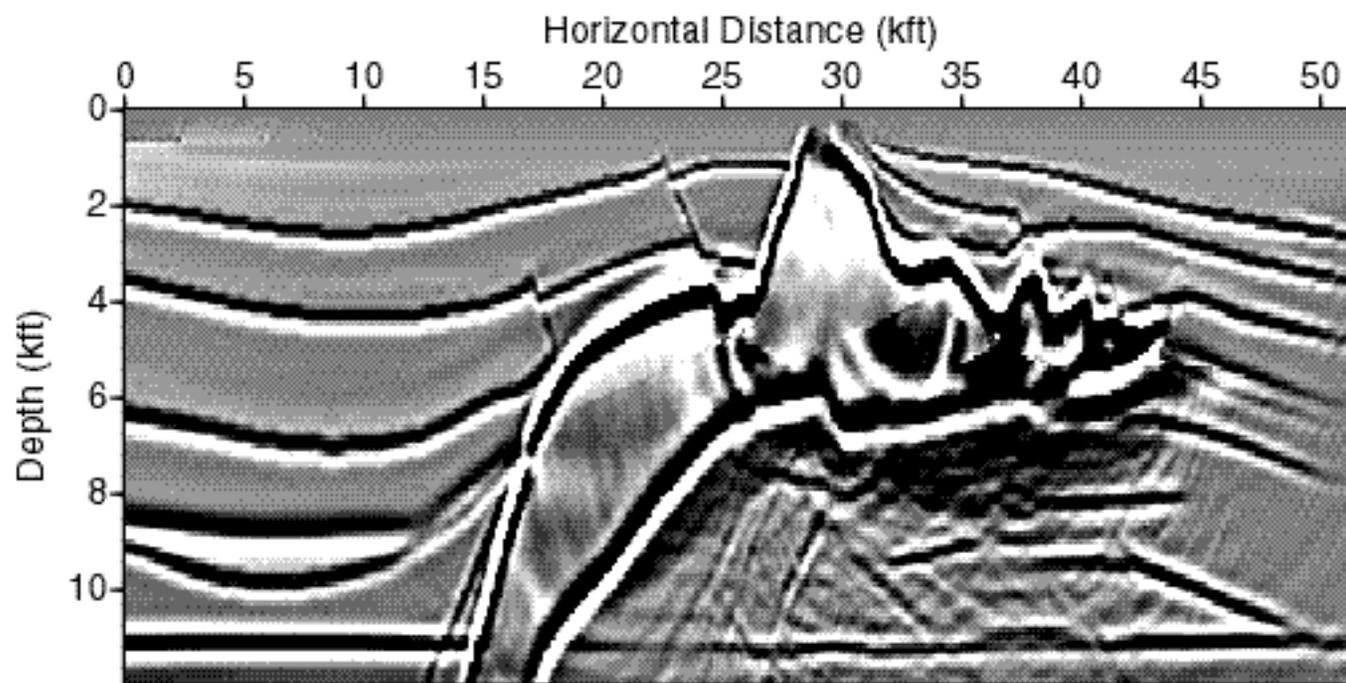
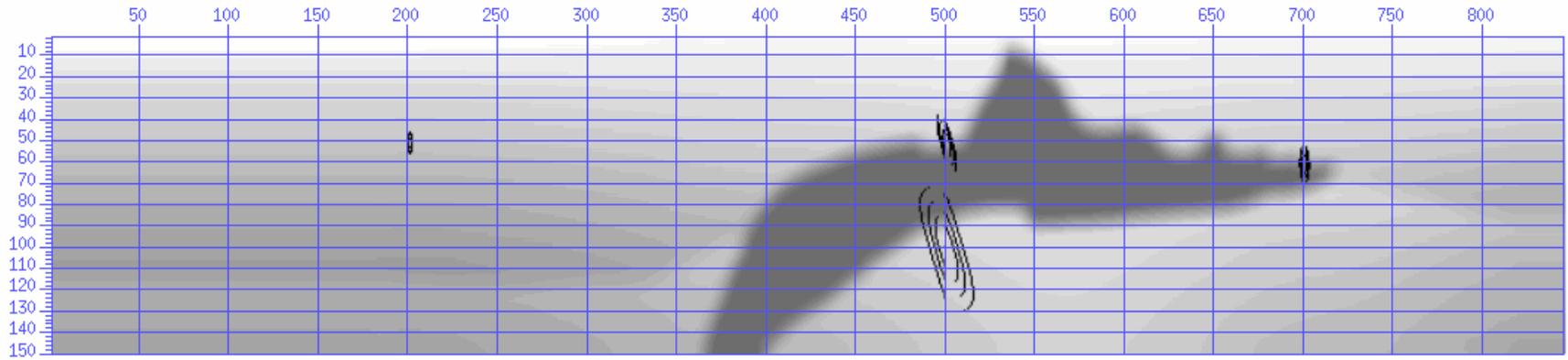


Image with  $\text{topw}=0.5$

# Investigation of Image Quality

- Image Resolution

- » Gives information about position error and limits on reservoir size

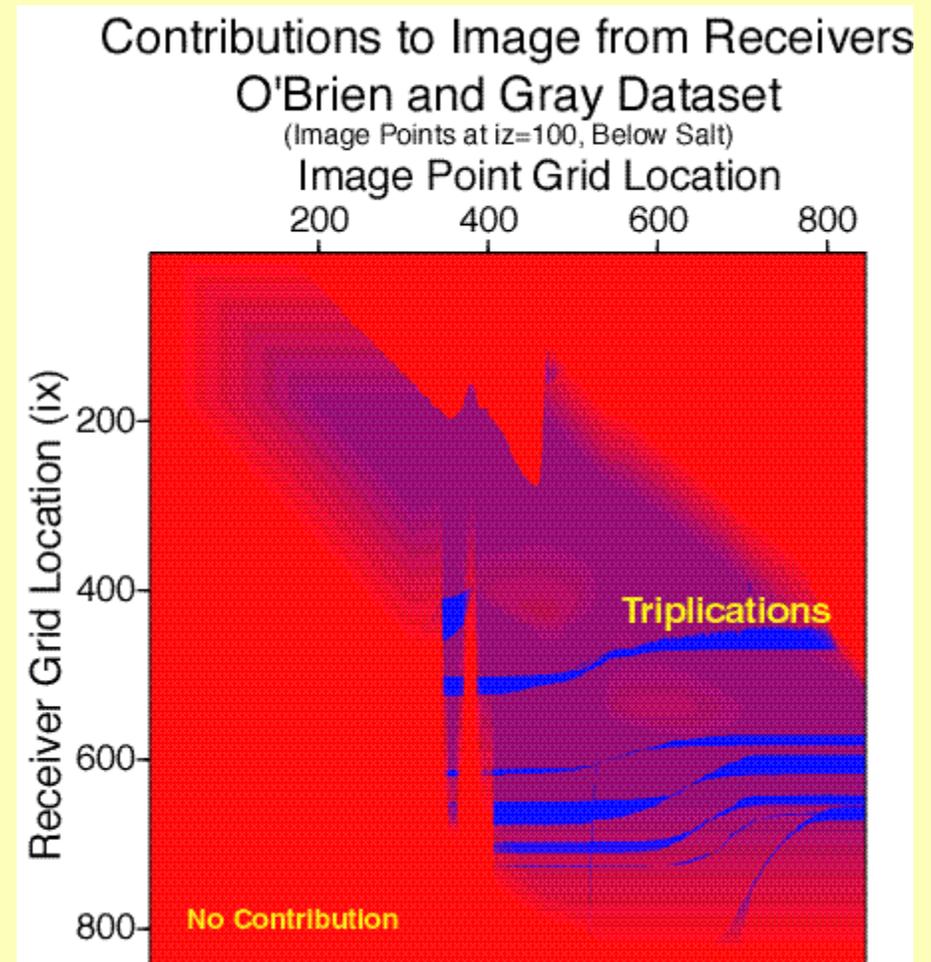


lascuatro

# Investigation of Image Quality

- Contribution of data to Image

- » Help design data acquisition
- » Want to maximize receiver aperture for best image



# Schedule of FY00 Work

FY 00 means May 2000 - May 2001 (FE Fiscal year)

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- Investigate what gives best images
  - » First arrivals
  - » Multiple arrivals
  - » Maximum amplitude
  - » Paths that avoid or travel through salt
  - » Shortest path length

# Scheduled FY00 Work

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- Development of quantitative measures of image resolution and quality
  - » Resolution function
  - » Data contribution histograms
  - » Semblance measure of image quality

# Cost for 3D Seismic Exploration

(Estimated by Bill French, costs per square km)

Acquisition: \$7,000

Processing: \$1,200

Prestack Migration: \$2,000

Interpretation: \$240

*Our Goal is to maximize information from  
acquisition and migration while improving  
drilling success*

# Kirchhoff Migration is Important

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- Many unresolved issues
  - » Improvements will lead to better imaging and better success in drilling
  - » Quantitative estimates of image quality will be useful
- Our studies transcend scale and geometry
  - » Applicable to interwell regimes
- Industry has shown great interest in our work